



A modelling study of the impact of cirrus clouds on the moisture budget of the upper troposphere

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**Cirrus dehydration
potential**

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A modelling study of the impact of cirrus clouds on the moisture budget of the upper troposphere

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Abstract

We present a modelling study of the effect of cirrus clouds on the moisture budget of the layer wherein the cloud formed. Our framework simplifies many aspects of cloud microphysics and collapses the problem of sedimentation onto a 0-dimensional box model, but retains essential feedbacks between saturation mixing ratio, particle growth, and water removal through particle sedimentation. The water budget is described by two coupled first-order differential equations for dimensionless particle number density and saturation point temperature, where the parameters defining the system (layer depth, reference temperature, amplitude and time scale of temperature perturbation and initial particle number density, which may or may not be a function of reference temperature and cooling rate) are encapsulated in a single coefficient. This allows us to scale the results to a broad range of atmospheric conditions, and to test sensitivities. Results of the moisture budget calculations are presented for a range of atmospheric conditions (T : 238–205 K; p : 325–180 hPa) and a range of time scales τ_T of the temperature perturbation that induces the cloud formation. The cirrus clouds are found to efficiently remove water for τ_T longer than a few hours, with longer perturbations ($\tau_T \gtrsim 10$ h) required at lower temperatures ($T \lesssim 210$ K). Conversely, temperature perturbations of duration order 1 hour and less (a typical timescale for e.g., gravity waves) are not found to efficiently dehydrate over most of the upper troposphere. A consequence is that (for particle densities typical of current cirrus clouds) the assumption of complete dehydration to the saturation mixing ratio may yield valid predictions for upper tropospheric moisture distributions if it is based on the large scale temperature field, but this assumption is not necessarily valid if it is based on smaller scale temperature fields.

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1. Introduction

Water vapor is the atmosphere’s most important greenhouse gas (e.g. Held and Soden, 2000) and condensed water in clouds strongly affects the Earth’s radiation balance. Hence, understanding water distribution in, and transport through, the atmosphere is an important aspect of understanding the climate system. Here, we present a modelling study that addresses the impacts of cirrus clouds on the moisture budget of upper tropospheric air masses. Specifically, we explore the relation between the time scales of atmospheric motions that induce clouds and the time scales of water removal by the sedimenting ice particles, and the efficiency of cirrus cloud dehydration at various levels of the upper troposphere.

The formation of ice particles through homogeneous or heterogeneous nucleation, their subsequent growth and sedimentation provide a challenge to any modelling effort, and the net effect of a cirrus cloud on the water vapor budget of an atmospheric layer often strongly depends on a large number of parameters and boundary conditions. These include, but are not restricted to: temperature and relative humidity profiles, aerosol concentrations and the air masses’ temperature history, on both long timescales (determining the available amount of water) and short (relevant for nucleation). Consequently, a broad range of phenomena are observed in the atmosphere, often associated with very specific atmospheric conditions. For example, Hall and Pruppacher (1976) showed how ice particles could survive a fall over several kilometers in subsaturated air, giving rise to so-called ‘fall-streaks’. Their study, however, also showed that such phenomena can occur for a limited range of relative humidity profiles and initial particle sizes only.

Given the strong and non-linear coupling of particle nucleation, particle number density, growth/evaporation of particles, and sedimentation fall speeds, models may be required to track individual ice crystals as they fall through the atmosphere in order to accurately model cloud evolution and the vertical redistribution of water. Such models have been successfully applied to denitrification in the polar vortex (Fueglistaler et al.,

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2002) and for the modelling of thin cirrus near the tropical tropopause (Luo et al., 2003; Jensen and Pfister, 2004). However, since these models were tailored to address very specific questions, they are not suited to address more general questions regarding typical dehydration timescales of cirrus clouds. Studies addressing issues of moisture transport on the large scale therefore often employ highly simplified cloud physics (e.g. Pierrehumbert, 1998; Dessler and Sherwood, 2000; Fueglistaler et al., 2005), which introduces uncertainty in their results regarding the order of magnitude of errors brought in by these simplifications.

In order to obtain a better understanding of typical timescales of cirrus clouds, and their implications for modelling moisture transport, we employ a simplified model of the water budget of an upper tropospheric layer. We neglect details of the microphysics but retain the important couplings between particle growth/evaporation, saturation mixing ratio and water depletion through sedimentation of particles. We consider only cases where ice crystals nucleate in the layer of interest, and exclude cases (for example convective anvils) where nucleation and growth occur under very different atmospheric conditions than particle sedimentation.

The model calculations are used to evaluate a) whether the dehydration is *fast* or *slow*, and b) the *efficiency* of the cloud to dehydrate the air mass, where *efficient* means that the layers' terminal mixing ratio is close to, or equal to, the minimum saturation mixing ratio of its temperature history.

Section 2 describes the model physics. Section 3 shows the evolution of the layer water budget for specific scenarios. In Sect. 4 we define a dehydration efficiency and calculate it for the range of reference temperatures and perturbation time scales typical of the upper troposphere. Section 5 provides a discussion of the applicability of the model results to the atmosphere, and of the model limitations. Finally, Sect. 6 summarizes the conclusions.

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2. Model description and model parameters

The 0-dimensional model employed here describes the water budget of an atmospheric layer with depth h . Most of the results shown are based on the assumption of homogeneous ice nucleation following the parameterization based on water activity by Koop et al. (2000), where we used simplifications similar to the ‘fast growth’ scenario by Kärcher and Lohmann (2002). However, in Sect. 4.3 we show that the overall character of these results is not very sensitive to this assumption, and that our conclusions can be scaled to include heterogeneous nucleation.

Once formed, particles are assumed to be in equilibrium with the surrounding gas phase, an assumption well justified for the cases discussed here with relatively high particle number densities, such that diffusive equilibration is a fast process (time scale of minutes) compared to the time scale of the temperature perturbations (hours). The available water vapor is equally distributed among all particles in the layer, giving rise to a uniform, monodisperse particle size distribution in the layer. Hence, the model does not resolve the complexities of a condensed water flux resulting from ice particles with a spectrum of fall velocities, but it does retain the important coupling between temperature (and hence saturation mixing ratio) and particle size and associated fall speed.

The water loss due to gravitational settling of the particles is calculated using the Locatelli and Hobbs (1974) parameterization of fall velocities as function of crystal size. Once a cloud is present in the layer, no new ice nucleation is assumed to occur, and the particle number density decreases as the particles fall out of the layer. This may lead to a small bias in particle sizes towards larger values (since the available water vapor during the cooling phase is distributed among fewer particles), and consequently the condensed water flux is somewhat overestimated.

As the temperature perturbation of the air mass is prescribed, the calculations ignore radiative impacts on the clouds. Possible impacts of radiation on the conclusions derived from the model calculations are discussed in Sect. 5.1.1.

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The model formalism is presented in the Appendix, and we discuss here some input parameters that deserve special attention.

2.1. Temperature perturbation δT

We prescribe isobaric temperature perturbations leading to the formation of cirrus clouds as harmonic oscillations around a reference temperature T_{ref} . The period of the oscillation (and hence the time scale of the temperature perturbation) is τ_T , ΔT is its amplitude, and $\delta T(t)$ denotes the temperature deviation at time t from the reference temperature T_{ref} , i.e.

$$\begin{aligned}\delta T(t) &= T(t) - T_{\text{ref}} \\ &= -\Delta T \cdot \sin(2\pi t / \tau_T), 0 \leq t \leq \tau_T / 2.\end{aligned}\quad (1)$$

Note that we have chosen to restrict t to the ‘cold phase’ of the temperature oscillation only. For these computations we associate a pressure $p(T_{\text{ref}})$ with each value of T_{ref} taken from a typical measured sounding during cirrus events at the Atmospheric Radiation Measurement Program (ARM) site Oklahoma.

The dependence of the model equations on ΔT is complex because this parameters enters the model in various ways. In most calculations we use $\Delta T = 2$ K, a simplification in order to keep the number of free variables as low as possible. A discussion of results for varying ΔT is provided in Sect. 4.1.

2.2. Layer depth h

Obviously, there is not a single number that can be assigned to the layer depth h based on firm physical grounds. Note that h is not the thickness of the cloud; rather it is merely the scale of the layer in which we assume particles nucleate, grow and eventually leave through sedimentation. The treatment of the layer as a homogeneous ‘box’ requires sufficiently homogeneous conditions within that box, which puts an upper bound to h of a few hundred meters. A deeper layer would not only have very inhomogeneous

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temperatures due to the vertical lapse rate or inhomogeneities in relative humidity, but would also be strongly affected by vertical wind shear over the time scales considered here.

We have therefore assigned a value of $h=300$ m, which we consider as a sensible value, with a possible range at different atmospheric conditions of about a factor two. Section 4.3 shows how the results may be scaled to account for variability in h .

2.3. Initial particle number density n_0

Homogeneous nucleation of ice particles depends on the cooling rate at the time when the critical saturation is reached, and therefore inherently depends on short time scale temperature fluctuations. In order to simplify and render the calculations comparable with one another, we specify conditions at time $t=0$ (when $\delta T=0$) such that nucleation immediately sets in. Hence, the cooling rates at the time of nucleation are

$$dT/dt(t=0) = -\Delta T \frac{2\pi}{\tau} \text{ [K/h]}, \quad (2)$$

that is for an amplitude $\Delta T=2$ K and a period $\tau_T=2$ h the cooling rate at the time of nucleation is ~ -6 K/h.

We compute the initial ice particle number density n_0 [cm^{-3}] at each temperature for these cooling rates from the [Kärcher and Lohmann \(2002\)](#) parameterization. This parameterization yields a maximum of $n_0 \approx 1.0 \text{ cm}^{-3}$ at $T_{\text{ref}}=205$ K, $p=179$ hPa and $\tau_T=1$ h, and a minimum of $n_0 \approx 0.001 \text{ cm}^{-3}$ at $T_{\text{ref}}=238$ K, $p=325$ hPa and $\tau_T=10$ h. These values compare well with observations, with a typical value of 10^{-1} cm^{-3} , ranging from 10^{-3} cm^{-3} to 10^1 cm^{-3} (see e.g. observations compiled by [Dowling and Radke, 1990](#)).

Note that coupling of particle nucleation to the cooling rate derived from the temperature perturbation leads to perhaps artificially small values of n_0 for very long time scales (i.e. $\tau_T \sim 10$ h). In reality, shorter period temperature perturbations with higher cooling rates (see e.g. [Hoyle et al., 2005](#)) and heterogeneous nucleation would then

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dominate the particle formation. Consequently, the calculations tend to underestimate n_0 , and hence overestimate the sedimentation velocity, for long τ_T . This point that will be discussed in Sect. 4.3 below.

2.4. The scaling parameter P

- 5 As shown in the Appendix, in our approximation the differential equations governing the system at fixed ΔT depend on a single nondimensional parameter P that encapsulates the temperature perturbation time scale τ_T , layer depth h , and initial particle number density n_0 :

$$P \equiv \frac{\tau_T}{2\pi h/v(r_0)} \equiv \frac{\tau_T}{2\pi\tau_{\text{fall}}}, \quad (3)$$

- 10 where $v(r)$ is the sedimentation velocity of a particle of effective size r , and r_0 is a particle radius scale involving the initial ice particle density and ΔT (see Appendix). Since in our simple model P governs the results, a wide range of values of the input parameters can be explored by simply relating them to the associated value of P and looking-up the results shown below for that specific value of P .

- 15 Figure 1 shows the dependence of P for $\Delta T=2$ K on τ_T and reference temperature T_{ref} for values characteristic of the upper troposphere. The two time scales are similar ($\tau_T \approx \tau_{\text{fall}}$) for $P \approx 0.16$. For P much greater than this value the sedimentation time scale is much shorter than τ_T , and we say that the dehydration is *fast*. Conversely, for $P \lesssim 0.1$ the sedimentation time scale is long compared to τ_T , and the dehydration is *slow*.
 20 Figure 1 shows that the conditions in the upper troposphere encompass both regimes, with values of P ranging from order 0.01 to 10. Under upper tropospheric conditions cirrus dehydration is in the *fast* regime ($P \gg 0.16$) for all $\tau_T \gtrsim 3$ h at $T_{\text{ref}} \approx 235$ K, increasing to all $\tau_T \gtrsim 10$ h at $T_{\text{ref}} \approx 210$ K. Similarly, cirrus dehydration is in the *slow* regime for all $\tau_T \lesssim 1$ h at $T_{\text{ref}} \approx 235$ K, increasing to all $\tau_T \lesssim 4$ h at $T_{\text{ref}} \approx 210$ K.

- 25 Figure 2 shows the contours of P for fixed $n_0=0.1 \text{ cm}^{-3}$. The overall character of the P contour pattern is very similar to that of the homogeneous nucleation scenario

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as shown in Fig. 1. For high T_{ref} and/or long τ_T the number of ice crystals nucleated homogeneously is less than 0.1 cm^{-3} , so P contours have moved to the right in Fig. 2. At lower T_{ref} and/or shorter τ_T the reverse is true; P contours have moved to the left.

The impact of increasing n_0 on P is seen in Fig. 3, where the $P=0.16$ contour is shown for fixed $n_0=0.1, 0.5$ and 1 cm^{-3} . For the lowest n_0 value only the lower left hand portion of the τ_T, T_{ref} graph falls into the *slow* regime, whereas for only a factor of 10 increase in particle density most of the upper troposphere would correspond to values in this regime. This implies an important role for ice nuclei in the hydrological cycle of the upper troposphere.

3. Cloud evolution

To facilitate comparison among model results at different reference temperatures, we express the total water content of the cloud layer in terms of the saturation point temperature T^* and its difference from the reference temperature, $\delta T^*(t) \equiv T^*(t) - T_{\text{ref}}$, rather than in terms of the mixing ratio in the layer. At a given pressure and given total water content the saturation point temperature T^* is the temperature at which the air would be exactly saturated with respect to ice (Betts et al., 1982).

Results are presented in terms of the non-dimensionalized deviations of temperature and of saturation point temperature from T_{ref} ,

$$\delta \hat{T}(t) \equiv \delta T(t) / \Delta T \quad (4)$$

and

$$\delta \hat{T}^*(t) \equiv \delta T^*(t) / \Delta T. \quad (5)$$

The number density of ice particles left in the layer at time t is $n(t)$ and the fraction of originally nucleated particles that remains in the layer is $\hat{n}(t) \equiv n(t) / n_0$ (see also Appendix).

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Figure 4 shows the evolution of $\delta\hat{T}$ and $\delta\hat{T}^*$ as functions of the non-dimensionalized time $\hat{t} \equiv 2\pi t / \tau_T$ for each of the (T_{ref}, τ_T) conditions shown by a colored dot in Figs. 1 and 2.

All cases for which $P < 0.16$ (dashed curves) are in the *slow* regime. That is, particle sedimentation is slow compared to the time scale of the temperature perturbation. Figure 4 shows that for these cases the layer, indeed, slowly dehydrates, and that the total moisture at $t = \tau_T/2$ (before the onset of the warming phase) is only marginally reduced by the cirrus cloud. Figure 4 further shows how the character of the cloud impact on layer dehydration changes in the transition region $P \approx 0.16$ where the two time scales τ_T and τ_{fall} are similar. (See the two turquoise curves, corresponding to $P = 0.1$ and $P = 0.2$ in these figures.) The cases with $P \geq 1$ are clearly in the *fast* regime.

All cases with $P \geq 1$ experience complete fall-out before $t = \tau_T/2$; however, their terminal moisture content shows an interesting, non-monotonic dependence on P . One might expect that for *faster* dehydration the final moisture content should always decrease. Figure 4 shows that for the cases with $P \geq 1$ (purple, yellow and red; solid curves) this is not the case. Rather, in these cases the fall-out is so fast that all particles have left the layer before the temperature minimum is reached. This is in part due to the low bias of the calculated n_0 at long time scales τ_T as discussed in Sect. 2.3, and Sect. 4.3 shows that this behaviour largely vanishes when the bias in n_0 is corrected.

Our discussion of specific scenarios has highlighted the role of P in determining whether dehydration is *fast* or *slow*. We have touched upon the relation between P and the final moisture content at time $t = \tau_T/2$, which is the focus of the next section.

4. Dehydration efficiency

We define the dehydration *efficiency* ϵ of a cloud as the amount of water actually removed by the cloud during a given isobaric cooling perturbation, divided by the maximum water made available for gravitational removal by that perturbation. Using the

previously introduced notation, ϵ is defined as

$$\epsilon \equiv \frac{Q(T^*(\hat{t} = \pi)) - Q(T^*(0))}{Q(T_{\text{ref}} - \Delta T) - Q(T^*(0))} \quad (6)$$

where Q is the total water vapor mixing ratio.

In cases for which $\epsilon \approx 1$, the cloud event removes the maximum possible water from the layer; i.e., at the end of the event the mixing ratio is close to the saturation mixing ratio at $T = T_{\text{ref}} - \Delta T$, whereas $\epsilon \approx 0$ indicates that the most of the ice particles re-evaporate within the layer.

Figure 5 shows that the cirrus clouds efficiently dehydrate the layer for high temperatures and time-scales τ_T longer than a few hours. As τ_T gets shorter, the dehydration efficiency decreases rapidly (depending on T_{ref}), and temperature perturbations shorter than ~ 1 h are too short to allow the particles to fall significantly at all. For fixed ΔT ϵ essentially depends on the governing parameter P only (see Appendix). Figure 5 shows this in that the contours of ϵ parallel those of P . The figure shows the previously noted increase of ϵ as P gets larger, with a slight decrease of ϵ at very high values of P .

Note that the $P=0.16$ curve lies very close to the $\epsilon=0.5$ contour, so that the *fast* and *slow* regimes correspond to $\epsilon > 0.5$ and $\epsilon < 0.5$, respectively. This coincidence is closest for $\Delta T = 2$ K but does not change greatly for other values of ΔT .

4.1. Dependence of the dehydration efficiency on T_{ref} and ΔT

From the definition of ϵ it can be seen that it is almost independent of T_{ref} at constant P . For δT^* , $\delta T \ll T_{\text{ref}}$, we can linearize the expression for ϵ in Eq. (6), to yield

$$\epsilon \approx \frac{\delta \hat{T}^*(\hat{t} = 0) - \delta \hat{T}^*(\hat{t} = \pi)}{1 + \delta \hat{T}^*(\hat{t} = 0)} \quad (7)$$

In this equation T_{ref} enters implicitly through its influence on the value of $\delta \hat{T}^*$ at cloud initiation ($\hat{t}=0$). The term $\delta \hat{T}^*(\hat{t}=0)$ represents the supersaturation needed for nucleation to occur.

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The dehydration efficiency depends on ΔT in the following ways. The sedimentation velocity scale $v(r_0)$, and hence P (Eq. 3), depend on the maximum available condensed-phase water, as well as on the initial particle number density n_0 . The maximum available condensate depends on T_{ref} and ΔT . Further, n_0 is a function of the cooling rate (and hence ΔT , see Eq. 2). Finally, the scaled initial condition, $\delta \hat{T}^*(\hat{t}=0)$, also depends on ΔT . Thus both the numerator and denominator of Eq. (7) depend on ΔT .

Figure 6 shows the dehydration efficiency as function of P and ΔT . For $P > 1$ the efficiency is near unity for all ΔT , but for small P the efficiency decreases with increasing ΔT ; the amount of water that falls out of the cloud does not increase as fast as does the maximum potential water loss as ΔT increases.

For $\Delta T = 2 \text{ K}$, $\epsilon(P)$ is well fit by the polynomial

$$\epsilon(P) = 3.58P - 6.99P^2 + 8.57P^3 - 6.22P^4 + 2.38P^5 - 0.36P^6. \quad (8)$$

This fit may be useful for studies of upper tropospheric humidity involving dehydration due to cirrus clouds. The change in total water content of an atmospheric layer due to clouds within it can be estimated as follows: When the critical supersaturation for nucleation is reached (no matter what its value is assumed to be), determine T_{ref} and τ_{T} (approximated for example by twice the time span until temperatures exceed T_{ref} again). Next, τ_{fall} is specified based on assumed n_0 and h (see Appendix). Now P is given by Eq. (3) which is inserted into the fit for ϵ (Eq. 8). Finally, Eq. (6) is rearranged to obtain the removed water

$$\begin{aligned} \Delta Q &= Q(T^*(\hat{t} = \pi)) - Q(T^*(0)) \\ &= \epsilon \cdot (Q(T_{\text{ref}} - \Delta T) - Q(T^*(0))). \end{aligned}$$

4.2. Sensitivity of ϵ to changes in P

For two reasons we are interested in examining the variations in ϵ due to uncertainties in P . First, the values of the parameters that determine P are not precisely known, and

hence introduce an uncertainty. Second, processes in the climate system that would systematically change the parameters that determine P , for example cloud particle number densities, would induce a change in ϵ . These variations of ϵ to changes in P can easily be derived from Eq. (8).

Figure 7 (solid line) shows the classically defined sensitivity $d\ln \epsilon/dP$, i.e. the fractional change of ϵ due to a given change in P . Evidently, the sensitivity is largest at small P , indicating that the dehydration efficiency of clouds in the *slow* regime is most sensitive, whereas the dehydration efficiency in the *fast* regime is largely insensitive to changes in P .

A somewhat different, but equally useful, quantity is the response $d\epsilon/d\ln P$ (not to be confused with the previous ‘sensitivity’) of ϵ to a relative change in P (Fig. 7, dashed line). One can argue that it is not so much the relative change in ϵ , but rather its absolute change, that is relevant here (because, for example, the climate system reacts to absolute changes in ϵ). Further, for at least some of the parameters determining P , the values may be known to within a certain factor, rather than an absolute value. The ‘response’ defined in this way shows a maximum at $P \approx 0.16$, i.e. where the two timescales τ_T and τ_{fall} are equal. The response decreases as P approaches both the *slow* and *fast* regime. In other words, dehydration remains inefficient in the *slow* regime, and remains efficient in the *fast* regime.

4.3. Scaling arguments

The results presented in the previous section were evaluated for $\Delta T = 2\text{ K}$, $h = 300\text{ m}$ and particle number densities for homogeneous nucleation parameterized in terms of maximum cooling rates. We now show that these results can be scaled to provide results for other parameter combinations.

In our simple model the parameters P and, to a lesser extent, ΔT , govern the evolution of the scaled saturation temperature (\hat{T}^*). Hence, for a given ΔT any parameter combination that yields the same value for P will have the same solution.

For example, the dehydration efficiency for an assumed depth $h = 600\text{ m}$ instead of

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300 m is readily read off from Fig. 6 by scaling τ_T correspondingly with a factor 2. The dehydration efficiency at a given reference temperature and a specific τ_X (for example 5 h) for the deeper cloud is then read off from Fig. 6 at the same reference temperature, but at $\tau_T=2\times\tau_X$ (in this case 10 h).

We have mentioned above that assuming homogeneous nucleation as function of $\delta T(t)$ yields very low values of n_0 at relatively high temperatures and/or long τ_T , which is a bit nonphysical, since it ignores the role of the (superimposed) high frequency temperature perturbations (Hoyle et al., 2005) and neglects any contribution of ice nuclei. These low n_0 values then artificially inflate the value of P leading to an apparent decrease in ϵ at long τ_T . Using the scaling properties of P , we may determine the impact of higher n_0 for these cases.

To determine the dehydration efficiency at $n_0=0.1\text{ cm}^{-3}$ for given T_{ref} , τ_T , we read off the P -value for those parameter values from Fig. 2, which we can denote $P=P_0$. Now, using Fig. 1 we find that τ_T at the same reference temperature for which $P=P_0$. Thus we have two equivalent situations, in which the difference in n_0 is compensated by a difference in τ_T . For example, to find the dehydration efficiency for the conditions corresponding to the large red dot of Fig. 2 ($T_{\text{ref}}=230\text{ K}$, $\tau_T=10\text{ h}$, $P_0=1$), we find the equivalent ($P_0=1$) homogeneous nucleation case in Fig. 1. This obtains for $T_{\text{ref}}=230\text{ K}$, $\tau_T\approx 5\text{ h}$, for which the dehydration efficiency (Fig. 6) $\epsilon\approx 1$, i.e. higher than in the homogeneous nucleation (coupled to the cooling rate proportional to τ_T) scenario.

Thus, a shift towards higher particle number densities induces a shift in P towards lower values, mitigating the previously noted peculiarity of slightly decreasing efficiencies at long τ_T . The decrease in ϵ with τ_T is thus shifted to very long temperature perturbations $\tau_T\gg 10\text{ h}$, which is (for most cases) of little relevance since cloud formation and evolution would occur by superimposed shorter temperature perturbations. Note that for the cases where the homogeneous nucleation scenario yielded $n_0>0.1\text{ cm}^{-3}$, the shift is in the other direction, towards higher values of P (faster). For example, the case $\tau_T=1\text{ h}$ and $T_{\text{ref}}=230\text{ K}$ (small red dot) has $P\approx 0.05$ in the homogeneous nucleation scenario, and $P\gtrsim 0.1$ for $n_0=0.1\text{ cm}^{-3}$.

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These results of this modelling study do not allow us to directly deduce conclusions about atmospheric moisture distribution, or, for example, frequency of cirrus cloud occurrence. Rather, these quantities must be determined by specific studies that prescribe the dynamic regime (e.g. mid-latitude frontogenesis, or subtropic large-scale descent) to determine the temperature history, and prescribe the water source terms (e.g. from moist convective updrafts, or mixing with moist layers). As pointed out in the introduction, the vertical cloud structure (and hence for example also the cloud's optical depth) might depend crucially on the relative humidities of the air masses below the layer studied here. If this layer were near saturation, one would expect a vertically thick cloud, whereas for a very dry layer the particles would immediately evaporate. Further, aspects such as cloud occurrence frequency may depend on nucleation thresholds and highly resolved temperature fields (e.g. Jensen and Pfister, 2004). In other words, cirrus cloud distributions and (vertical) structure depend crucially on the air masses' history in terms of temperature and moisture flux, and may be very sensitive to parameters such as particle number density or nucleation threshold.

What our scaling results, however, robustly predict, is that in the upper troposphere the atmosphere cannot hold more water than given by the saturation mixing ratio for temperature perturbations of order 1 h and longer at high temperatures (230 K), and longer than a few hours at very low temperatures (205 K). Conversely, typical sedimentation in cirrus clouds is too slow to substantially dehydrate upper tropospheric air masses for temperature perturbations shorter than these time scales. In practice, this means that the temperature field as resolved by large-scale atmospheric models combined with dehydration to the minimum saturation mixing ratio is a reasonable basis to study upper tropospheric moisture transport and distribution.

This has been implicitly assumed in previous studies which have shown empirically that model runs with complex and simple cloud microphysics yield similar results for the atmospheric moisture distribution. We believe that our study provides useful scaling

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arguments as to why this is the case in the upper troposphere.

5.1. Limitations

5.1.1. Radiation

In the formulation of our framework we have neglected effects of radiation, which may tend to destabilize a cloud layer through longwave cooling at the top, and longwave heating at the bottom. We have excluded these effects because of the large range of possibilities resulting from variable solar insolation, and, particularly, underlying cloud cover. Further, the impact of radiation depends on the cloud's optical depth, which in turn depends on its entire vertical structure, and not just the atmospheric layer with depth h . Our results have shown that for low temperatures, cirrus lifetimes of at least several hours are to be expected. These lifetimes are long enough to allow radiation to affect the evolution of the cirrus cloud. While we do not expect that radiative effects would entirely change the results of, for example, dehydration efficiency, we stress that these limitations should be borne in mind when applying the results to the real atmosphere.

5.1.2. Turbulence, wind shear and mixing

The implicit assumption of a 0-dimensional model as employed here is that the box's integrity is not affected over the time of the model evaluation. Turbulent mixing and wind shear, however, might be expected to invalidate this assumption particularly for the cases with longer time scales τ_T . While it is in principle possible to include effects of turbulent mixing with ambient air masses, one would have to introduce scenarios of the composition and temperature structure of these ambient air masses and the turbulent mixing time scale (which in turn might depend on the radiative heating/cooling of the cloud). Estimates of this time scale, based on measured turbulence spectra in the upper troposphere, vary over three orders of magnitude, ranging from minutes to many

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hours. Thus each case would have to be carefully assessed to determine the impact of turbulence on atmospheric dehydration via cirrus clouds. Such assessment is clearly beyond the scope of the treatment presented here, in which we present a limiting (zero-turbulence) case, yielding maximum water removal from the layer.

5 **6. Conclusions**

We have used a simple model to describe dehydration of an upper atmospheric layer by cirrus clouds that formed in-situ. Scaling arguments show that the results can be applied to a broad range of parameter values. Expected variability/uncertainty of these parameters under atmospheric conditions, and model limitations prevent applying the model results directly to specific observations. The model results do, however, provide general and useful insight into the dehydration potential of cirrus clouds in the upper troposphere.

The parameter combination P that governs the impact of cirrus clouds on the air mass moisture budget, is essentially the ratio of the temperature perturbation time scale to that of the ice particle sedimentation. We find that under typical upper tropospheric conditions, dehydration is *fast* for τ_T of order hours (and longer), or *slow* for shorter τ_T . More specifically, the results of our scaling study indicate that

- a) for the range of the governing parameters under current conditions, the upper troposphere cannot hold substantially more water than given by the saturation mixing ratio based on the larger-scale temperature field (This result would change if n_0 were a factor 10 or more larger than under present conditions);
- b) high frequency temperature perturbations $\tau_T < \tau_{crit}$ are too short to allow significant dehydration, with τ_{crit} being temperature dependent. At $T_{ref} = 235\text{ K}$ $\tau_{crit} \approx 1\text{ h}$ and at $T_{ref} = 205\text{ K}$ $\tau_{crit} \approx 7\text{ h}$;

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c) the dehydration efficiency decreases with increasing magnitude ΔT of the temperature perturbation for *slow* cases; it is independent of ΔT for *fast* cases.

The overall character of our results is independent of details of the ice nucleation mechanism, the cloud microphysics, the temperature fluctuation spectrum and/or the cloud depth. The major impact on our results of shifting any of these (for example, to higher nucleated ice particle density, to deeper clouds, or to a more complex representation of the particle size spectrum) is to simply shift the occurrence frequency of *fast* and *slow* regimes in the upper troposphere. For example, as n_0 increases strongly, the boundary between regimes is shifted in the τ_T/T_{ref} space, as shown in Fig. 3, but the general character of P and ϵ contours remains unchanged. Thus it may be argued that in a different climate regime, for example, in which n_0 and/or typical values of τ_T might change, the behaviors we have described would occur but in different regions of the atmosphere. In particular, the relationship between dehydration efficiency and P given by Eq. (8) would hold in another climate regime; however, the values of P and therefore of dehydration efficiency ϵ corresponding to fixed temperature and τ_T would change.

Our model, in conjunction with data on the frequency distribution of clear air humidity, and spectra of temperature perturbations, could be used to estimate the distribution of τ_T characteristic of the current upper troposphere. This would allow an assessment of the relative importance of the *fast* and *slow* regimes in today's atmosphere, a useful way to characterize the current state and predicted shifts in atmospheric behavior under changes in aerosols, greenhouse gases or other perturbations.

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Appendix A

The formalism

Equations for cirrus model

Let $Q(t)$ ($q_{\text{ice}}(t)$) be the total water (ice) mixing ratios (kg H₂O/kg air) in the cloud at time t :

$$Q(t) = q_{\text{vapor}}(t) + q_{\text{ice}}(t) \quad (\text{A1})$$

and let $n[m^{-3}](t)$ be the number density of ice crystals, all of the same radius r , in the cloud at time t .

Assume the temperature history:

$$T(t) \equiv T_{\text{ref}} - \Delta T \cdot \sin(2\pi \cdot t / \tau_T) \quad (\text{A2})$$

where τ_T is the period of the temperature oscillation, assumed isobaric, and $\Delta T[K]$ is its amplitude.

The cloud evolution equations are

$$\frac{dQ}{dt} = -q_{\text{ice}} \frac{v(r)}{h}, \quad q_{\text{ice}} > 0, \quad (\text{A3})$$

and

$$\frac{dn}{dt} = -n \frac{v(r)}{h} \quad (\text{A4})$$

where the sedimentation velocity of an ice particle of radius r is (Locatelli and Hobbs, 1974):

$$v(r) = C \cdot r^x. \quad (\text{A5})$$

C and x are constants depending on the flow regime (and consequently on the particle size), and r is a measure of the particle size.

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Now, we assume a monodisperse particle size distribution in the cloud layer (for discussion see Sect. 2), such that the ice water mixing ratio is approximately given by

$$q_{\text{ice}} = n \frac{4\pi}{3} \cdot \frac{\rho_{\text{ice}}}{\rho_{\text{air}}} \cdot r^3 \equiv B(n) \cdot r^3 \quad (\text{A6})$$

where ρ_{ice} is the density of solid ice and ρ_{air} that of air at the given temperature and pressure. Expressing the particle radius and fall velocity in terms of condensed water content, particle number density and ratio of densities yields

$$r = (q_{\text{ice}}/B(n))^{1/3}, v(r) = C(q_{\text{ice}}/B(n))^{x/3} \quad (\text{A7})$$

which we can insert into the time dependent equations for Q and n (Eqs. A3 and A4):

$$\frac{dQ}{dt} = -C \frac{q_{\text{ice}}^{(1+x/3)}}{h} \cdot \left(\frac{1}{B(n)} \right)^{x/3} \quad (\text{A8})$$

$$\frac{dn}{dt} = -C \frac{n}{h} \cdot \left(\frac{q_{\text{ice}}}{B(n)} \right)^{x/3} \quad (\text{A9})$$

Under the approximations of our model, we can express Q and q_{ice} as functions of the saturation point temperature T^* , defined for a layer of total water mixing ratio Q at pressure p as the temperature for which

$$Q = q_{\text{sat}}(T^*, p) \quad (\text{A10})$$

where q_{sat} is the saturation mixing ratio over ice. For small perturbations in temperature $\delta T \equiv T - T_{\text{ref}} \ll T_{\text{ref}}$ the Clausius-Clapeyron equation can be written

$$q_{\text{sat}}(T, p) \approx q_{\text{sat}}(T_{\text{ref}}, p) \exp(A(T_{\text{ref}}) \cdot \delta T) \quad (\text{A11})$$

where $A(T_{\text{ref}}) \equiv \frac{L_{\text{sub}}}{R_v T_{\text{ref}}^2}$ for L_{sub} [J/kg], R_v [J/kg/K], being the latent heat of sublimation and the gas constant for vapor, respectively. $A(T_{\text{ref}})$ varies between 0.1 and 0.14 over the temperature range considered here.

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Then the water conservation equation (Eq. A3) becomes an equation for δT^* :

$$\frac{d\delta T^*}{dt} = \frac{1}{A(T_{\text{ref}})} \frac{d \ln Q}{dt} \quad (\text{A12})$$

$$= -\frac{1}{A(T_{\text{ref}}) Q} \cdot C \frac{q_{\text{ice}}^{(1+x/3)}}{h} \cdot \left(\frac{1}{B(n)}\right)^{x/3} \quad (\text{A13})$$

and, assuming that in the presence of ice the cloudy air is exactly saturated with respect to ice,

$$q_{\text{ice}}(t) = q_{\text{sat}}(T_{\text{ref}} + \delta T^*(t), p) - q_{\text{sat}}(T(t), p) \quad (\text{A14})$$

$$\approx q_{\text{ice},0} \cdot (\delta \hat{T}^* - \delta \hat{T}) \quad (\text{A15})$$

where we define

$$q_{\text{ice},0} \equiv A(T_{\text{ref}}) \cdot \Delta T \cdot q_{\text{sat}}(T_{\text{ref}}). \quad (\text{A16})$$

It is convenient to nondimensionalize these equations. Let

$$\delta \hat{T}^* \equiv \delta T^* / \Delta T$$

$$\delta \hat{T} \equiv \delta T / \Delta T$$

$$\hat{t} \equiv \frac{2\pi t}{\tau_T}$$

$$\hat{n} \equiv \frac{n}{n_0}$$

$$q_{\text{ice}}^{\wedge} \equiv \frac{q_{\text{ice}}}{q_{\text{ice},0}}$$

$$\hat{r} \equiv \frac{r}{r_0}$$

where the particle radius scale is

$$r_0 \equiv \left(\frac{q_{\text{ice},0}}{B(n_0)} \right)^{1/3}. \quad (\text{A17})$$

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The time scale for fall-out is

$$\tau_{\text{fall}} \equiv \frac{h}{v(r_0)}. \quad (\text{A18})$$

Note that τ_{fall} depends on ΔT and on n_0 .

We define

$$P \equiv \frac{\tau_T}{2\pi \cdot \tau_{\text{fall}}}. \quad (\text{A19})$$

The non-dimensionalized equations then are, from Eqs. (A8) and (A4),

$$\frac{d\hat{n}}{d\hat{t}} = -P \hat{q}_{\text{ice}}^{x/3} \hat{n}^{(1-x/3)} \quad (\text{A20})$$

and

$$\frac{d(\delta\hat{T}^*)}{d\hat{t}} = -P \cdot \hat{q}_{\text{ice}}^{(1+x/3)} \cdot \hat{n}^{-x/3} \times \exp(-A(T_{\text{ref}})\Delta T \delta\hat{T}^*) \quad (\text{A21})$$

Equations (A20) and (A21) constitute our model. The initial conditions are $\hat{n}(0)=1$; $\delta\hat{T}^*(0)=\delta T_{\text{nuc}}^*/\Delta T$, where δT_{nuc}^* is that saturation temperature displacement required for nucleation.

The model equations and the initial conditions involve three parameters T_{ref} , ΔT and P . Over the range of temperatures considered here, $0.1 \leq A(T_{\text{ref}}) \leq 0.15$. Moreover, the nucleation temperature displacement remains in the range 3–3.2 K for $205 \text{ K} \leq T_{\text{ref}} \leq 235 \text{ K}$. Therefore the influence of variations in T_{ref} on our results is very small. On the other hand, the temperature perturbation amplitude ΔT determines the initial condition, it comes into the equations (see Eq. A21) and it determines the velocity scale $v(r_0)$, so, indirectly, the third parameter, P . In most of the results presented in this paper we focus on the influence of P at fixed ΔT , and we deal with the impact of variations in ΔT in Sect. 4.1.

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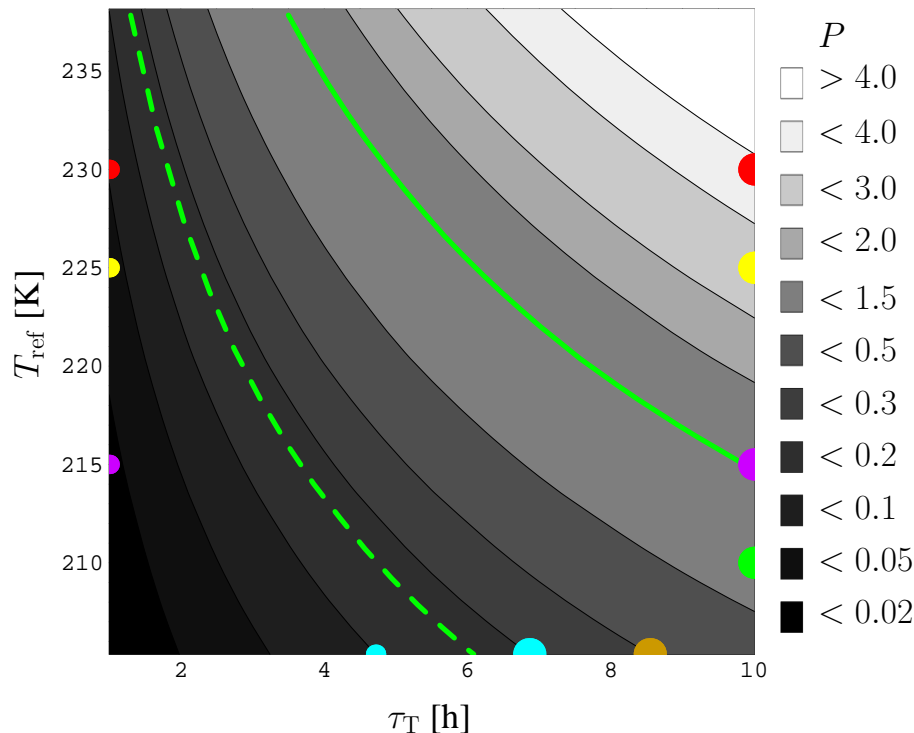


Fig. 1. The non-dimensional parameter P as function of T_{ref} and τ_T at $\Delta T=2\text{ K}$. Higher P values correspond to lighter gray values. The green dashed curve is $P=0.16$ and the green solid curve is $P=1$. Colored dots are the T_{ref} , τ_T values for cases discussed in Sect. 3. The P values associated with these dots are as follows: starting from the small red dot on the upper left and moving counterclockwise; $P=.05, .035, .015, 0.1, 0.2, 0.3, 0.64, 1.0, 2.5, 3.8$. Small dots correspond to $P \leq 0.16$ (slow regime) and large dots to larger P values (fast regime).

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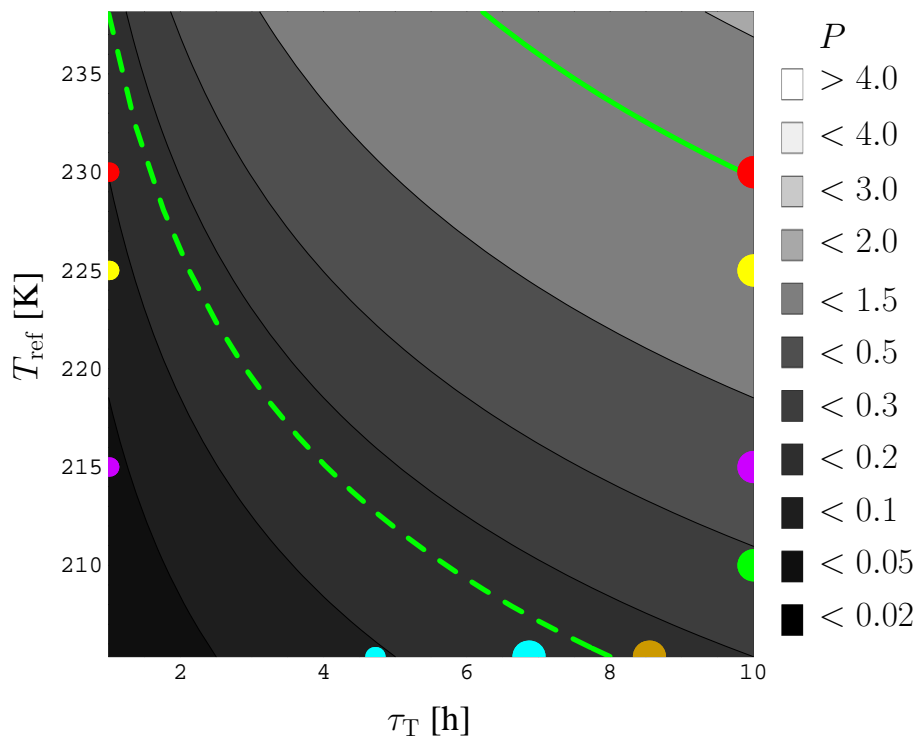


Fig. 2. Contours of P at fixed $\Delta T=2\text{ K}$ for fixed $n_0=0.1\text{ cm}^{-3}$. Color coding and contours as in Fig. 1.

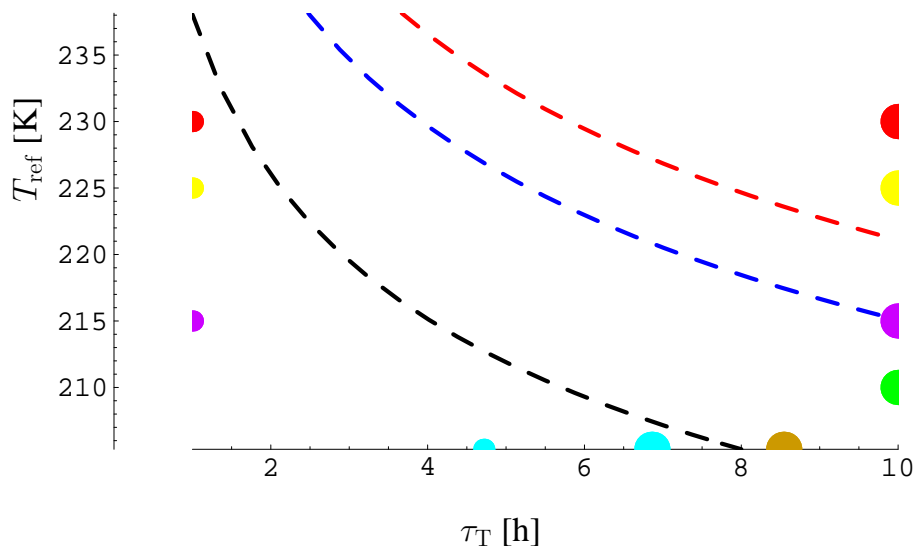
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Fig. 3. $P=0.16$ contour for fixed $n_0=0.1\text{ cm}^{-3}$ (black), $n_0=0.5\text{ cm}^{-3}$ (blue) and $n_0=1\text{ cm}^{-3}$ (red). As n_0 increases, more and more of the (T_{ref}, τ_T) range falls into the $P \leq 0.16$ (slow) regime, where clouds persist for most (or all) of the perturbation period.

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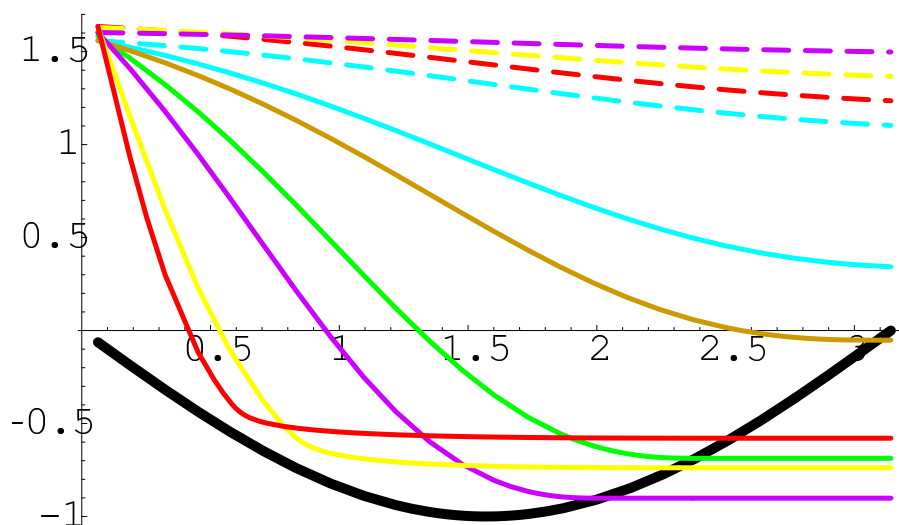


Fig. 4. Evolution of nondimensionalized temperature $\delta\hat{T}(\hat{t})$ (bold black) and of nondimensionalized saturation point temperature $\delta\hat{T}^*(\hat{t})$ over a single cooling event. Each curve corresponds to a (T_{ref}, τ_T) pair shown by a dot of the same color in Fig. 1. Dashed curves correspond to the small dots in that figure and solid curves to the larger ones.

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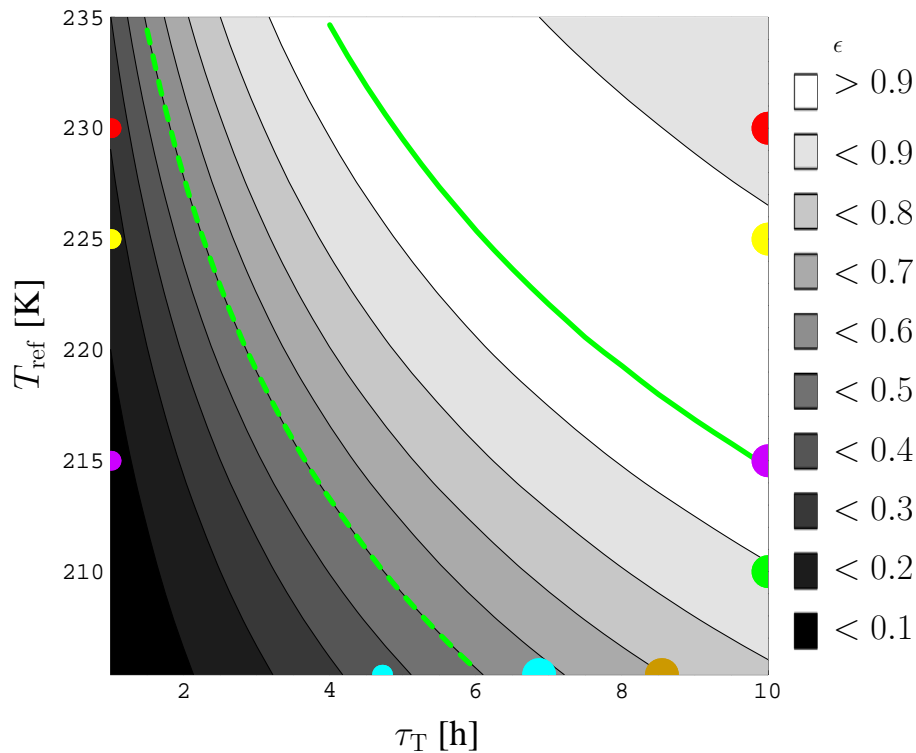


Fig. 5. The dehydration efficiency ϵ (see Eq. 6) for $\Delta T=2\text{ K}$ for the range of T_{ref} and τ_T shown in Fig. 1. $P=0.16, 1$ (green curves) and colored dots as in Fig. 1.

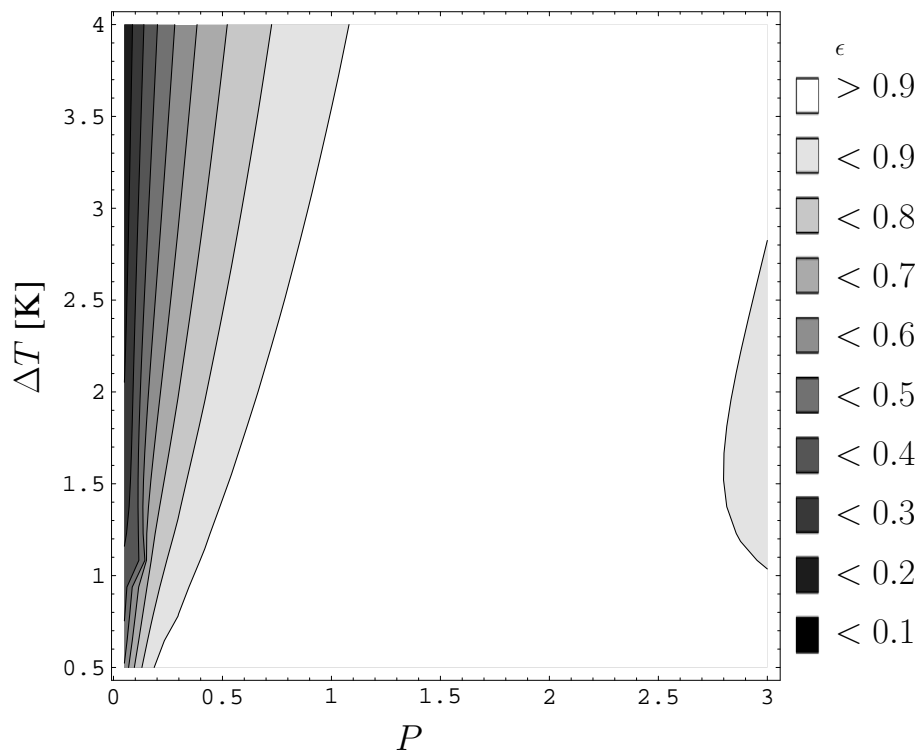
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Fig. 6. Dehydration efficiency ϵ for a range of values of ΔT and P , contours are as in Fig. 5.

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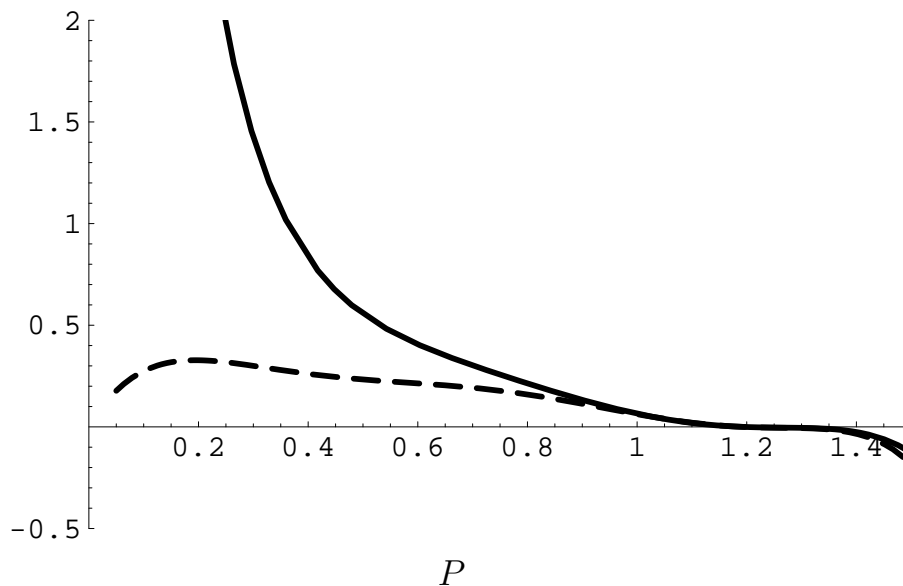
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Fig. 7. Two measures of the variation in dehydration efficiency ϵ to variations in P at constant $\Delta T = 2\text{ K}$: the response $R(p) \equiv d\epsilon/d \ln P$ (dashed), and sensitivity $S(p) \equiv d(\ln \epsilon)/dP$ (solid) for the full range of P values in this study.

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